



# INERTIALIZATION: HIGH-PERFORMANCE ANIMATION TRANSITIONS IN GEARS OF WAR

DAVID BOLLO  
PRINCIPAL SOFTWARE ENGINEER  
THE COALITION (MICROSOFT STUDIOS)



# ANIMATION TRANSITIONS





# ANIMATION TRANSITIONS

- Transition from one animation state to another
- Typically a cross-fade blend between poses



Source

Blend



Target







# ANIMATION TRANSITIONS

- Optimizations are often focused on the blend step
- Fast SLERP, optimizing cache and memory usage, etc



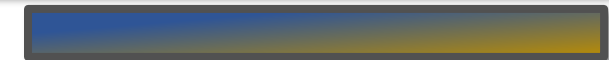
- Biggest cost is evaluating both Source and Target
- Source/Target cost is much greater than blend cost





# MULTIPLE CHARACTERS

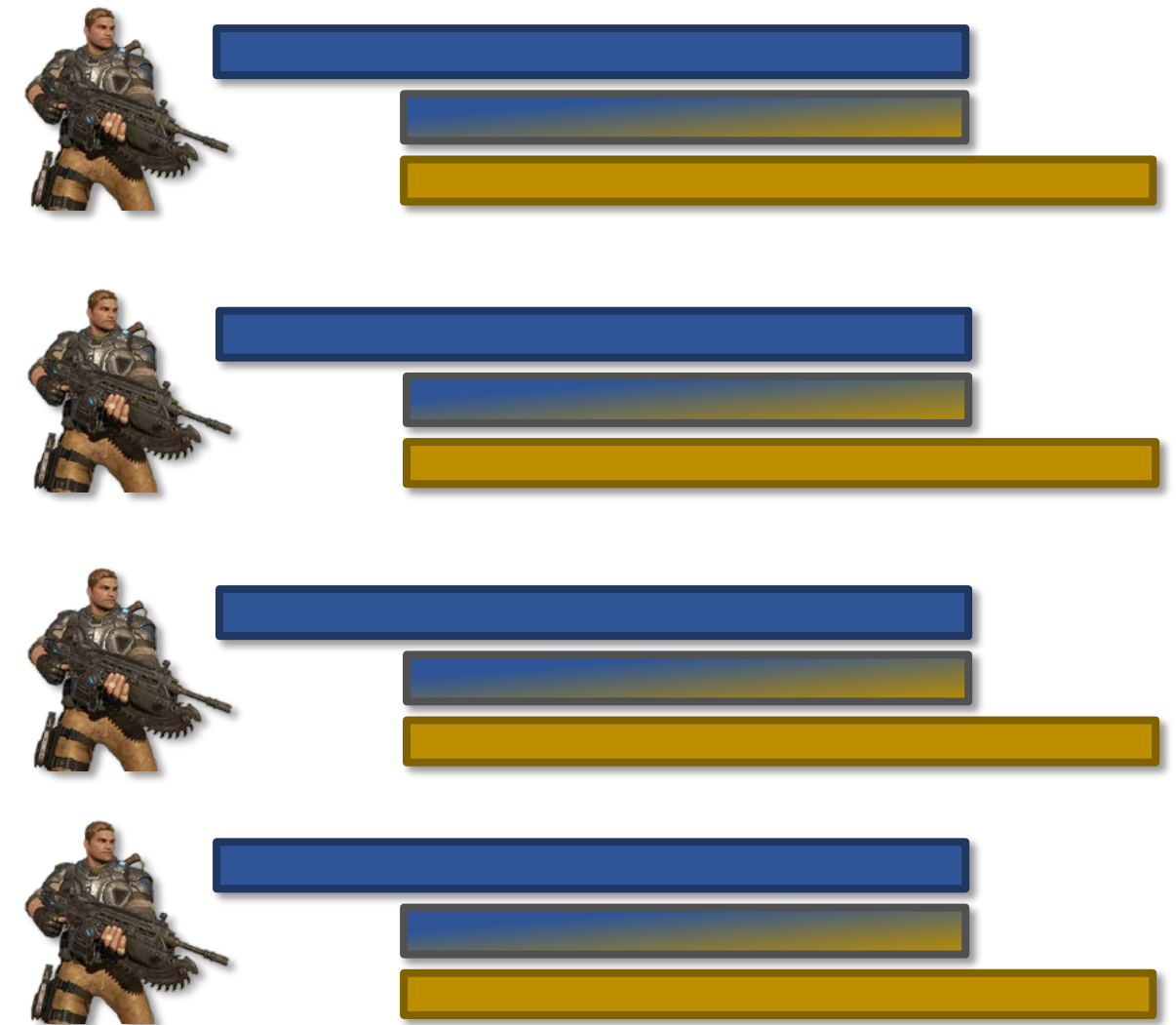
- If we're lucky...
- Only a few active transitions at once





# MULTIPLE CHARACTERS

- But in the worst case...
- Everybody transitions at the same time
- Double the animation cost







# CAN WE DO BETTER?

- Intuition: Real humans don't "blend"
- (but they do have inertia)



Source

Blend



Target







# CAN WE DO BETTER?

- IDEA: Eliminate blended transitions!
- Fix the discontinuities as a post-process



Source

Blend



Target





# CAN WE DO BETTER?

- IDEA: Eliminate blended transitions!
- Fix the discontinuities as a post-process



Source

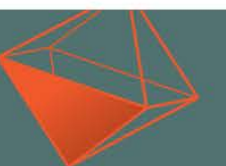


Target



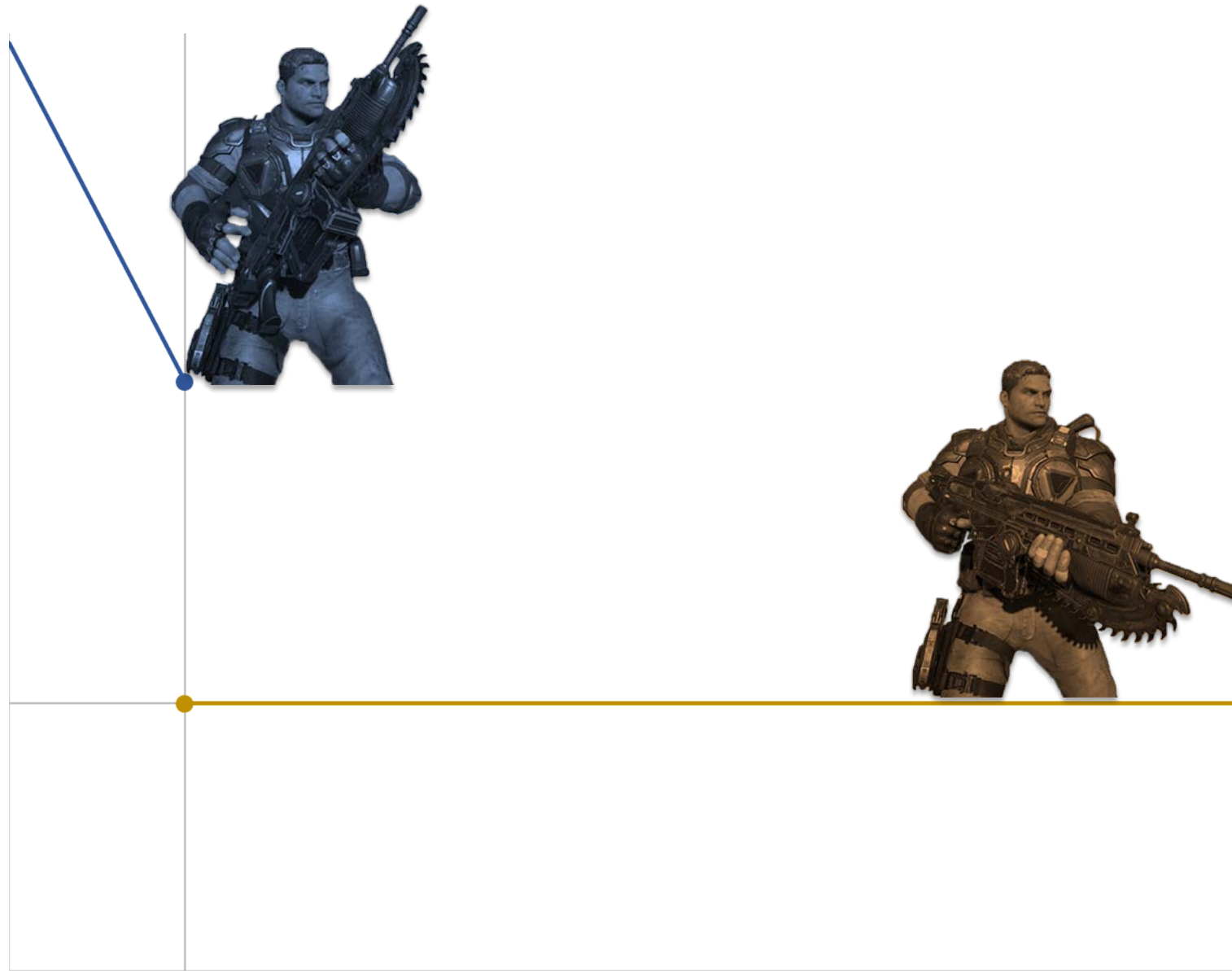


# TRANSITIONS AS A POST-PROCESS





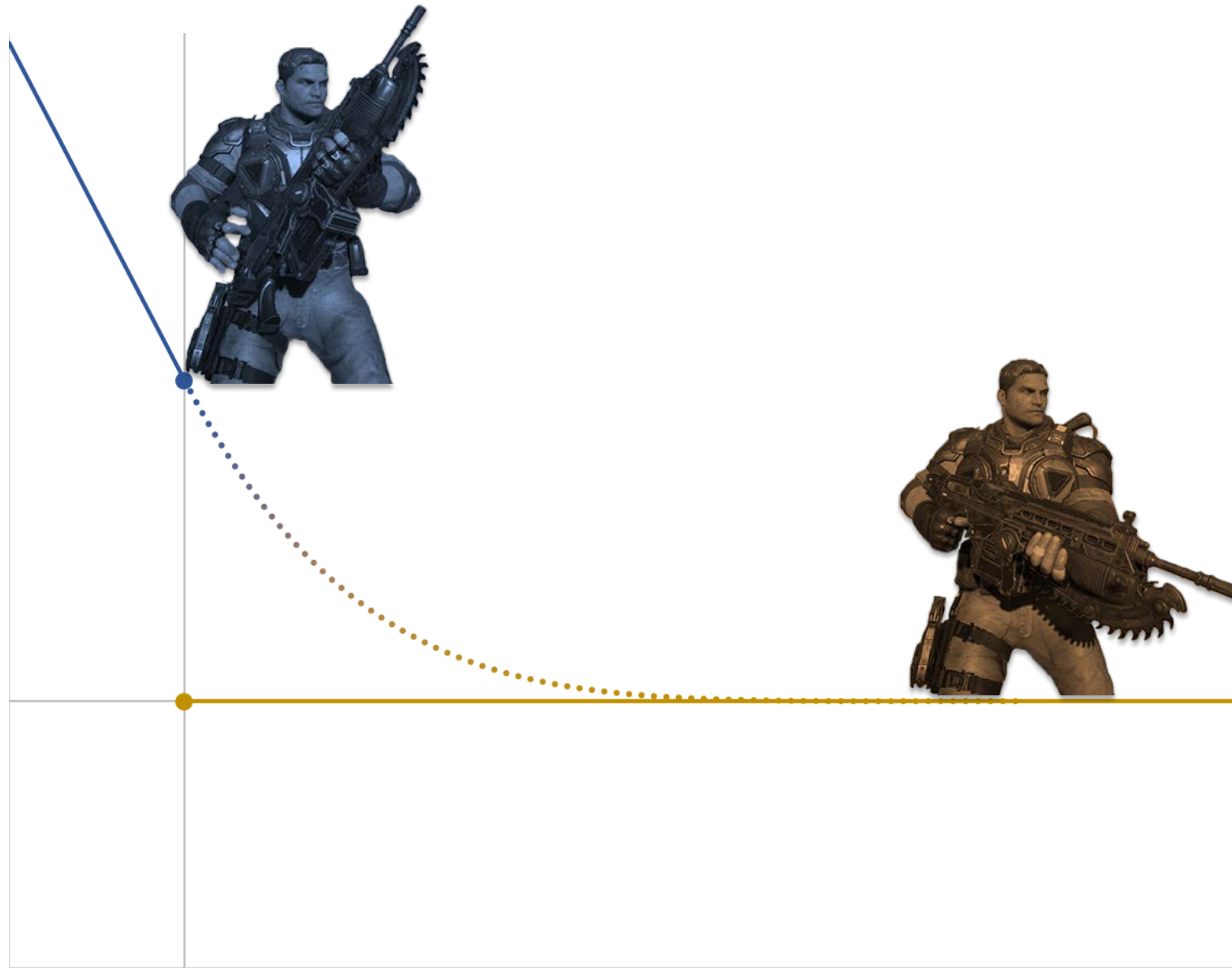
# TRANSITIONS AS A POST-PROCESS







# TRANSITIONS AS A POST-PROCESS





# GOALS

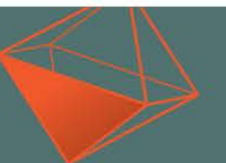
- **Respect** the original animation
  - No changes when not transitioning
- **Believable** and aesthetically pleasing
  - Smooth and momentum-preserving
- **Stay on-model**
  - No bad / unnatural poses
  - No overshoot





# IDEA #0: FILTER DISCONTINUOUS POSE

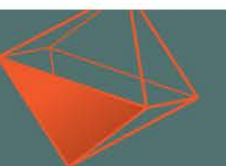
- Apply a filter to the output pose stream
- Difficult to tune
- Introduces lag
- Deviates from input even when not transitioning





# IDEA #1: BLEND FROM POSE

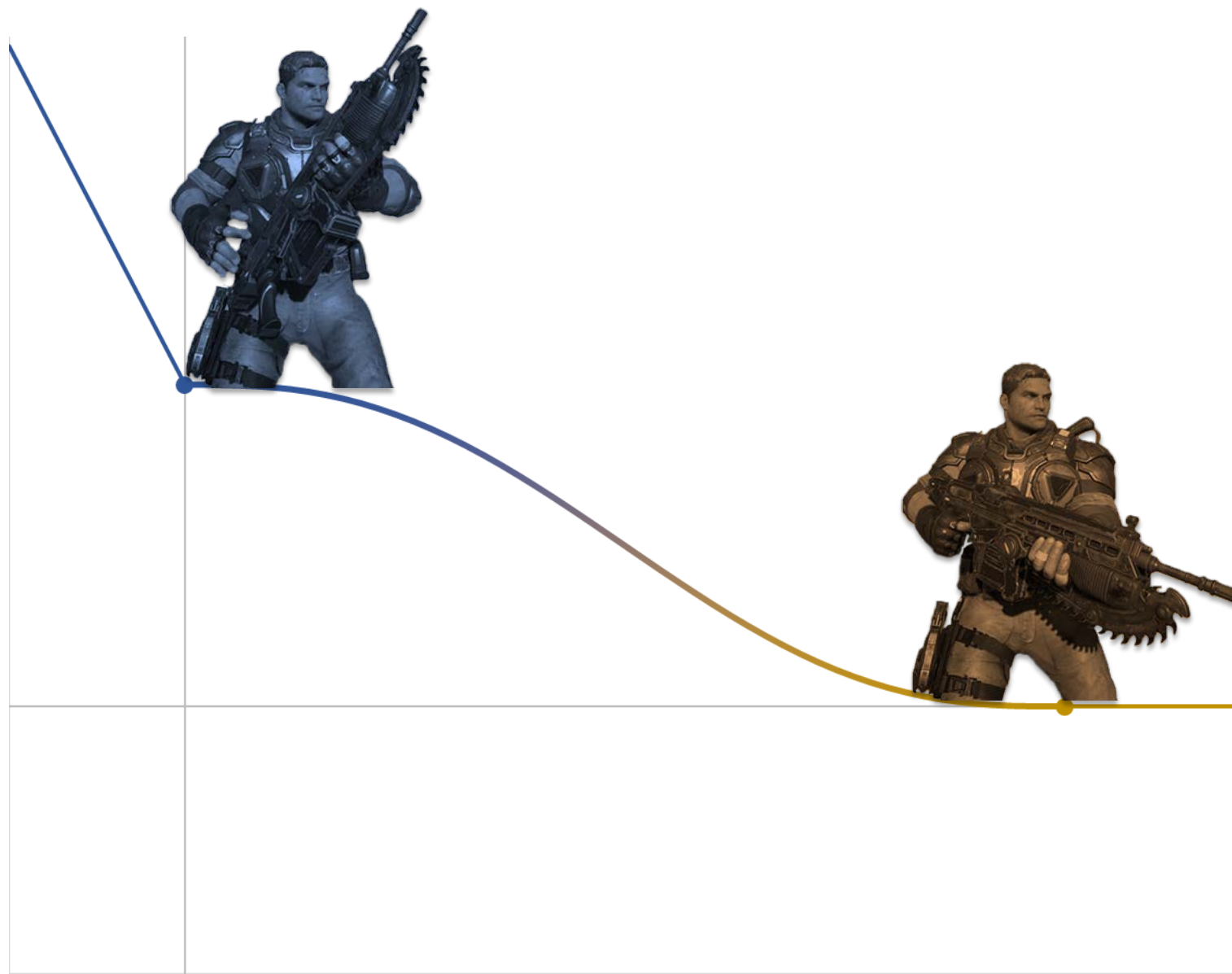
- Capture pose difference between Source and Target
- Ease out the difference over time







# IDEA#1: BLEND FROM POSE

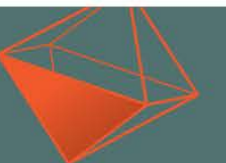




# IDEA #2: MATCH VELOCITY

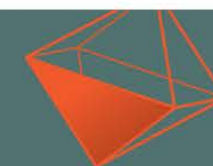
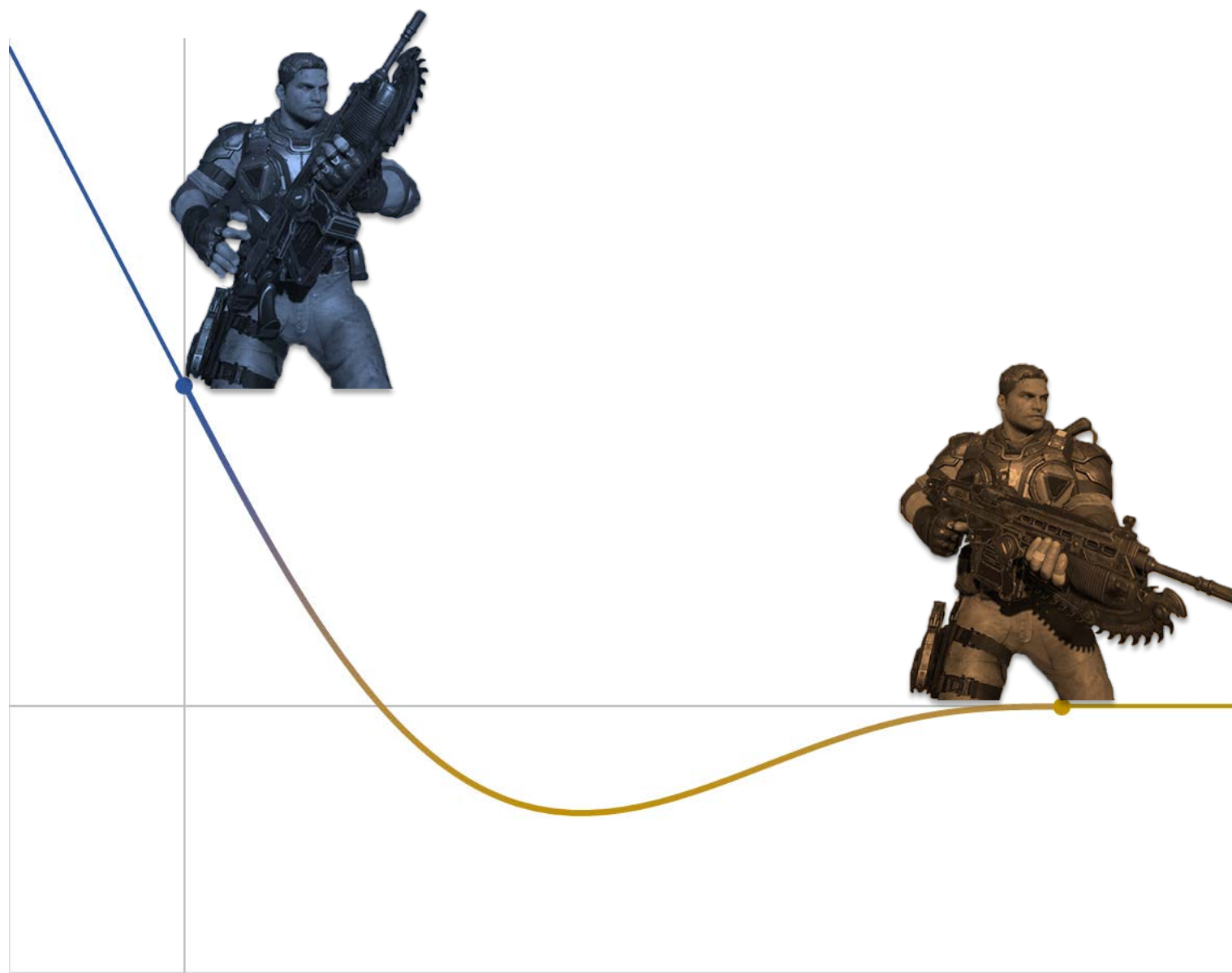
- Capture pose difference between Source and Target
- Ease out the difference over time
- Remember Source velocity (via finite differences)
- Match initial velocity
- Quintic polynomial [Flash and Hogan 1985]

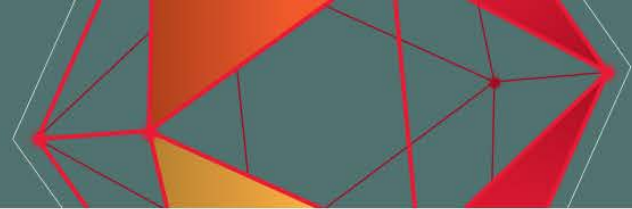
T. Flash and N. Hogan. 1985. The Coordination of Arm Movements: An Experimentally Confirmed Mathematical Model. *Journal of Neuroscience* 5, 7 (July 1985), 1688 – 1703





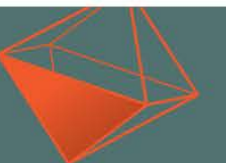
# IDEA #2: MATCH VELOCITY





# IDEA #3: LIMIT OVERSHOOT

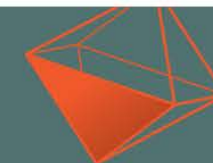
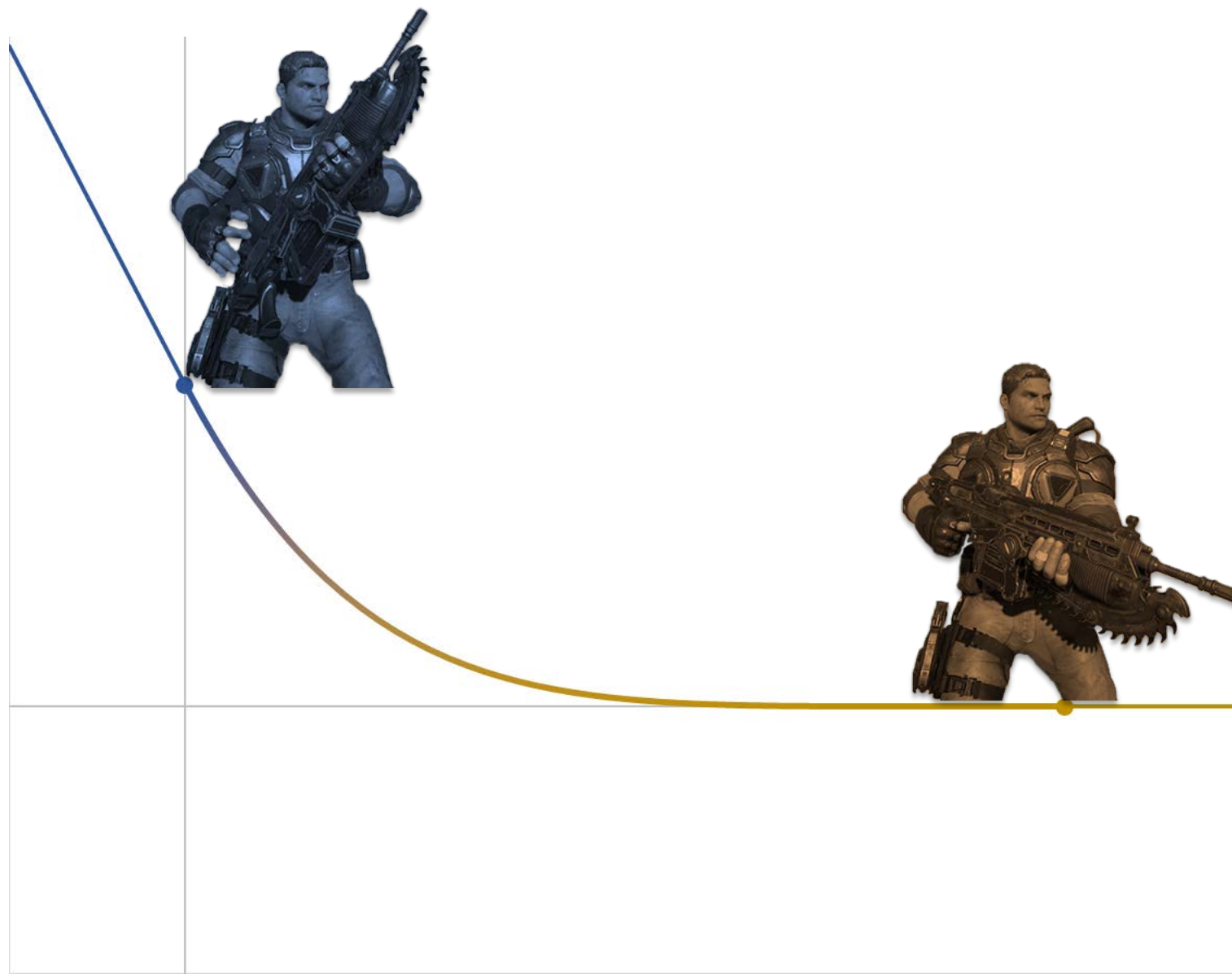
- Capture pose difference between Source and Target
- Ease out the difference over time
- Remember Source velocity (via finite differences)
- Match initial velocity
- Limit overshoot by controlling initial acceleration
- Choose  $a_0$  to give us zero jerk at  $t_1$





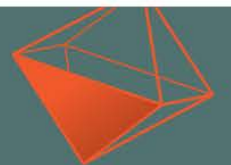


# IDEA #3: LIMIT OVERSHOOT



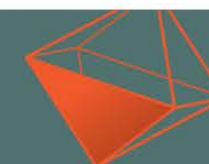
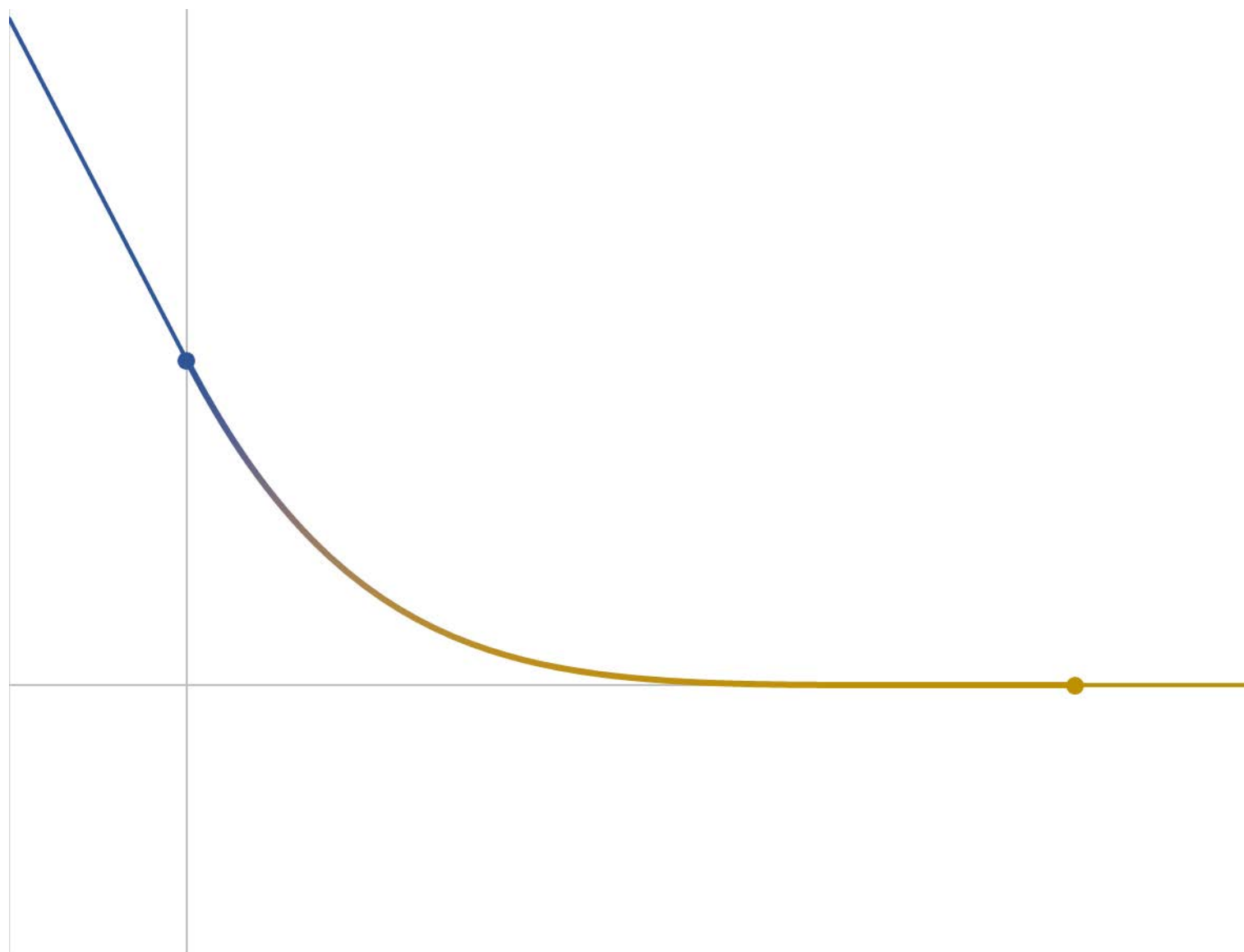


# I NERTIALIZATION



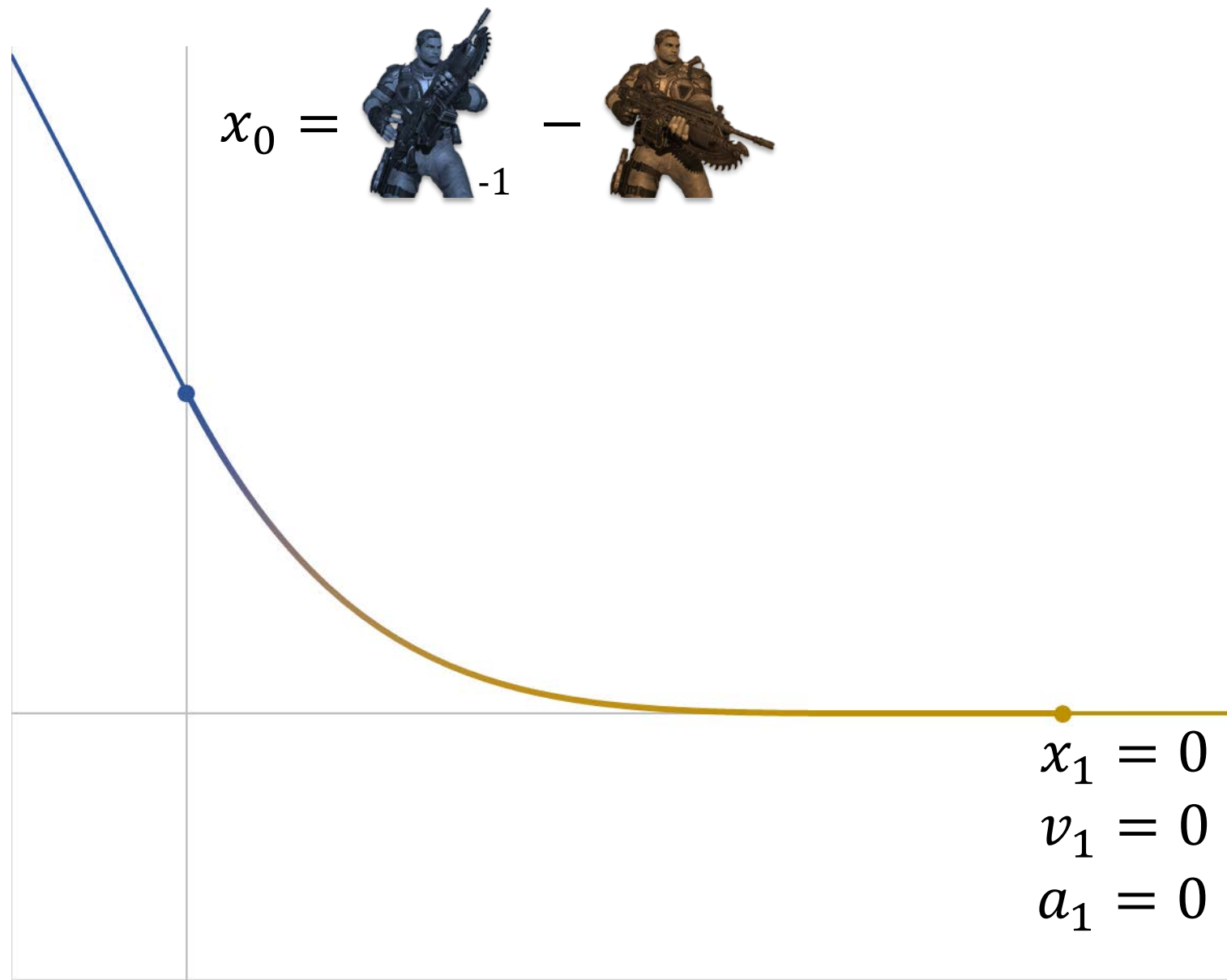


# INERTIALIZATION





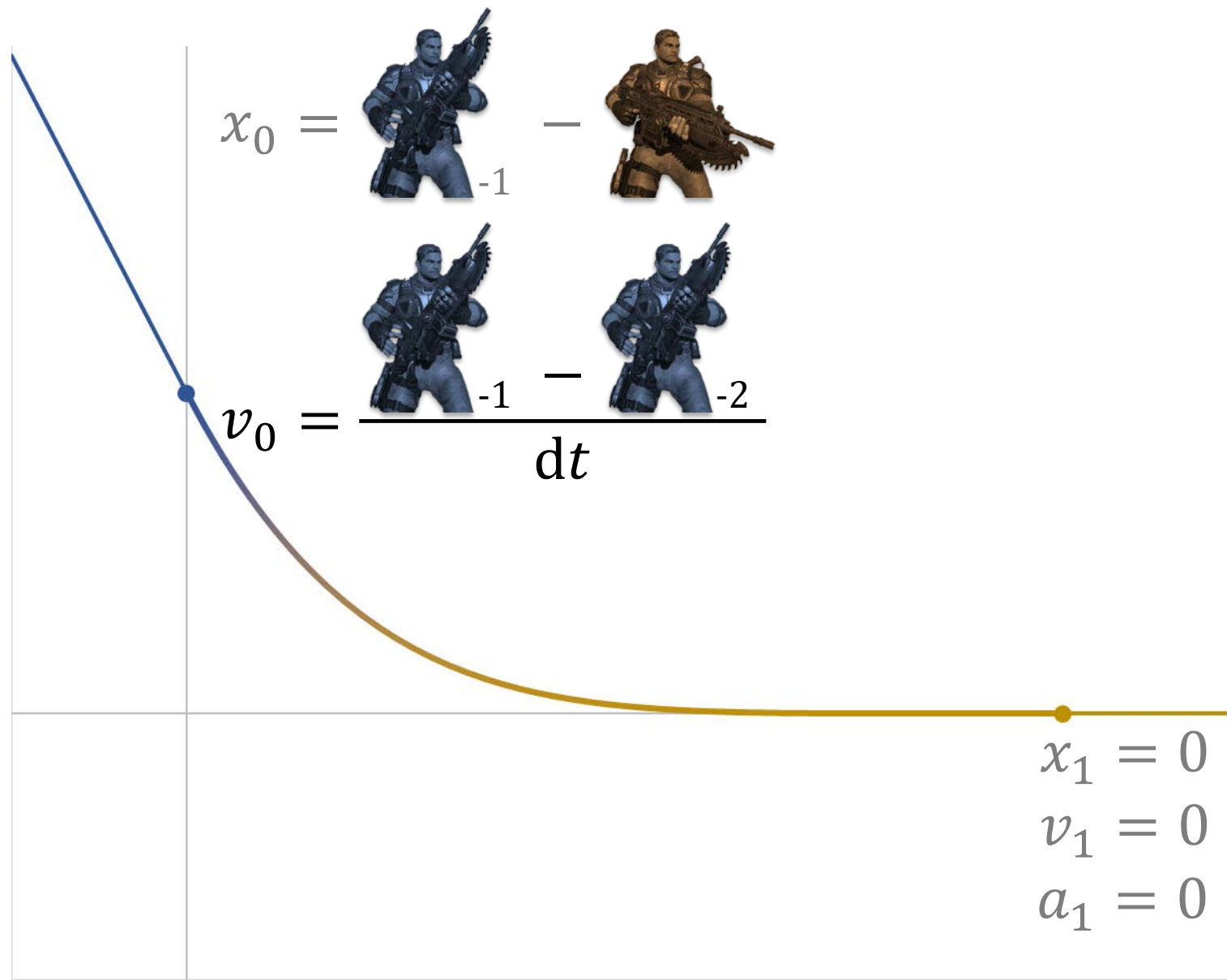
# INERTIALIZATION – INITIAL VALUES





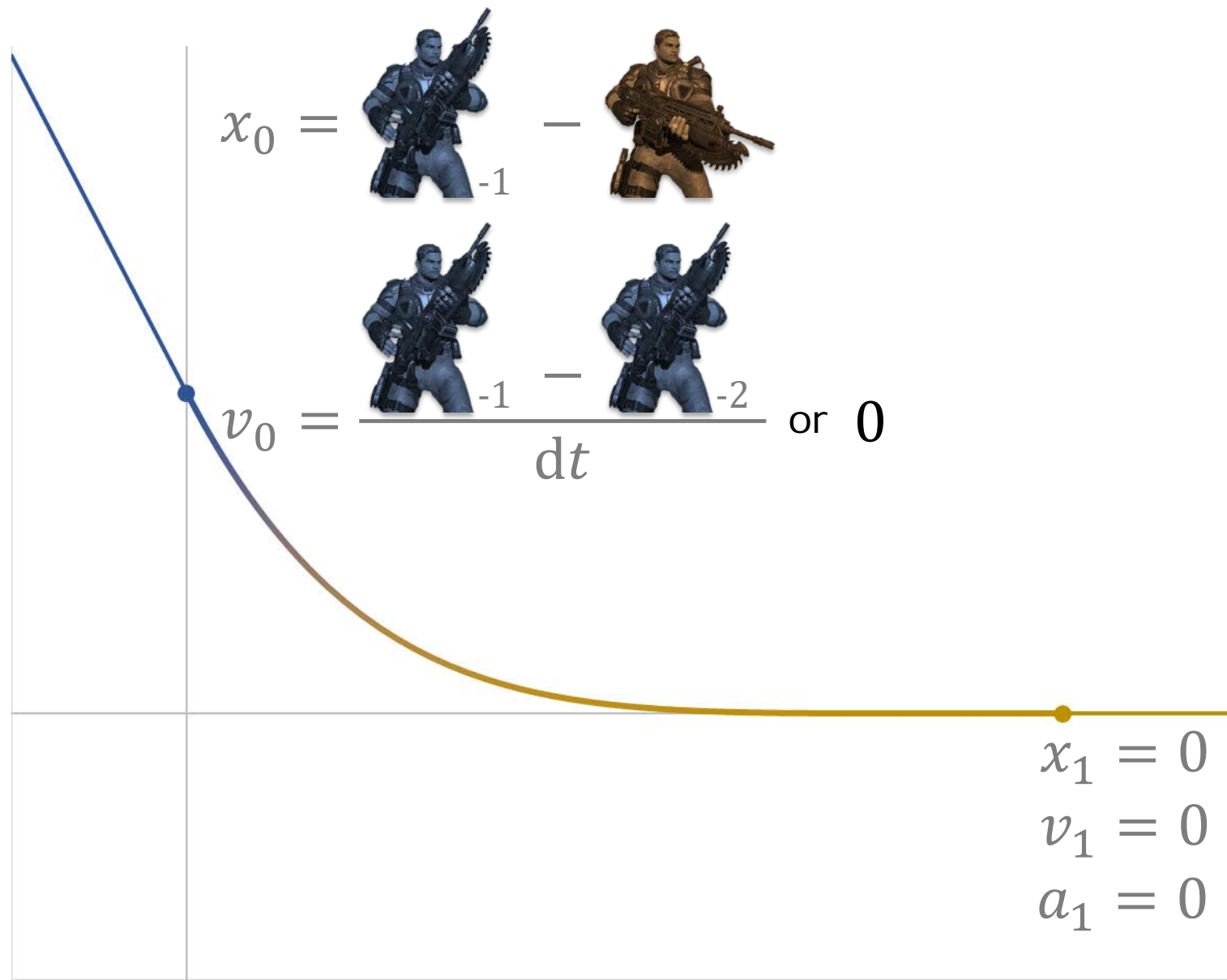


# INERTIALIZATION – INITIAL VELOCITY



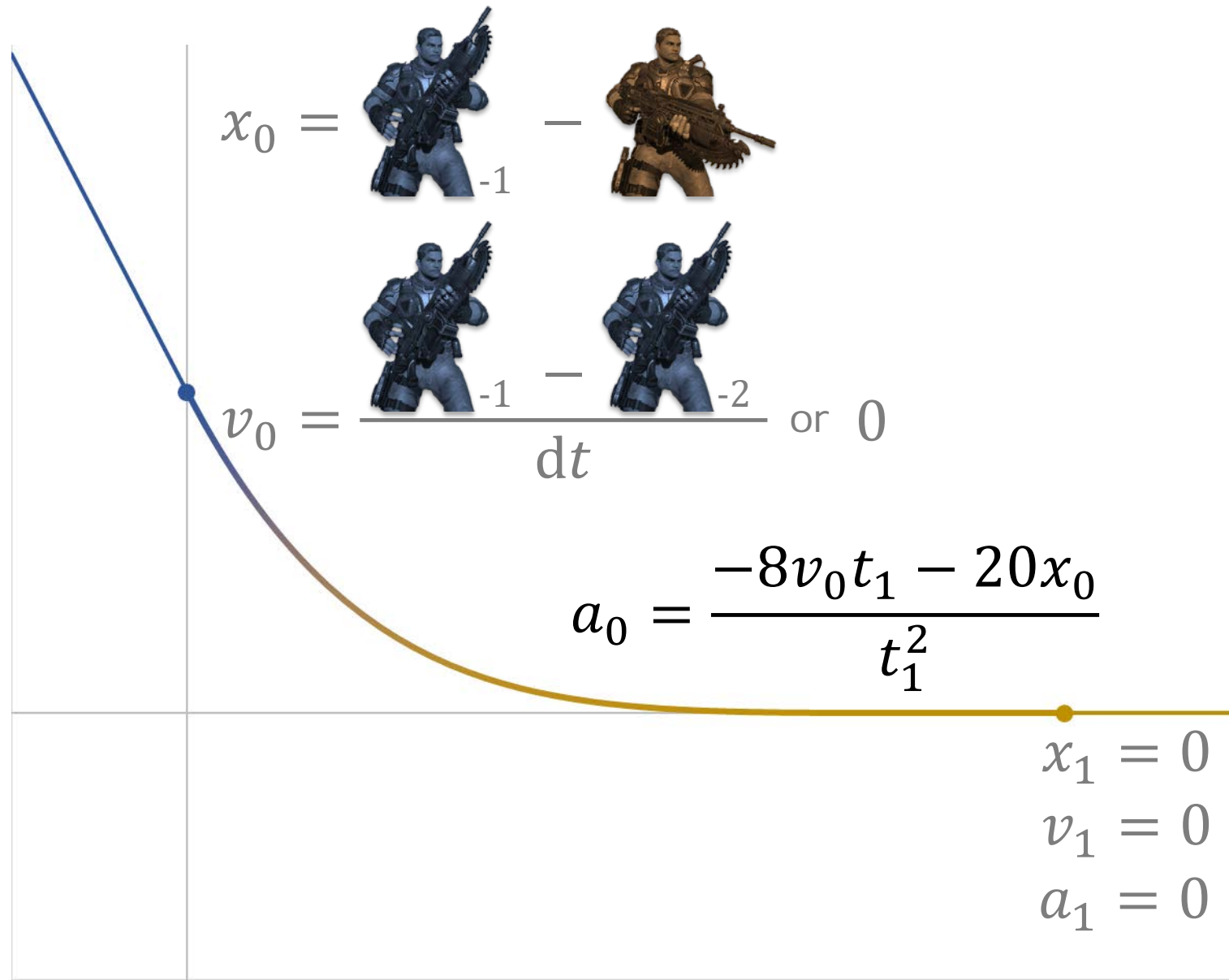


# INERTIALIZATION – INITIAL VELOCITY





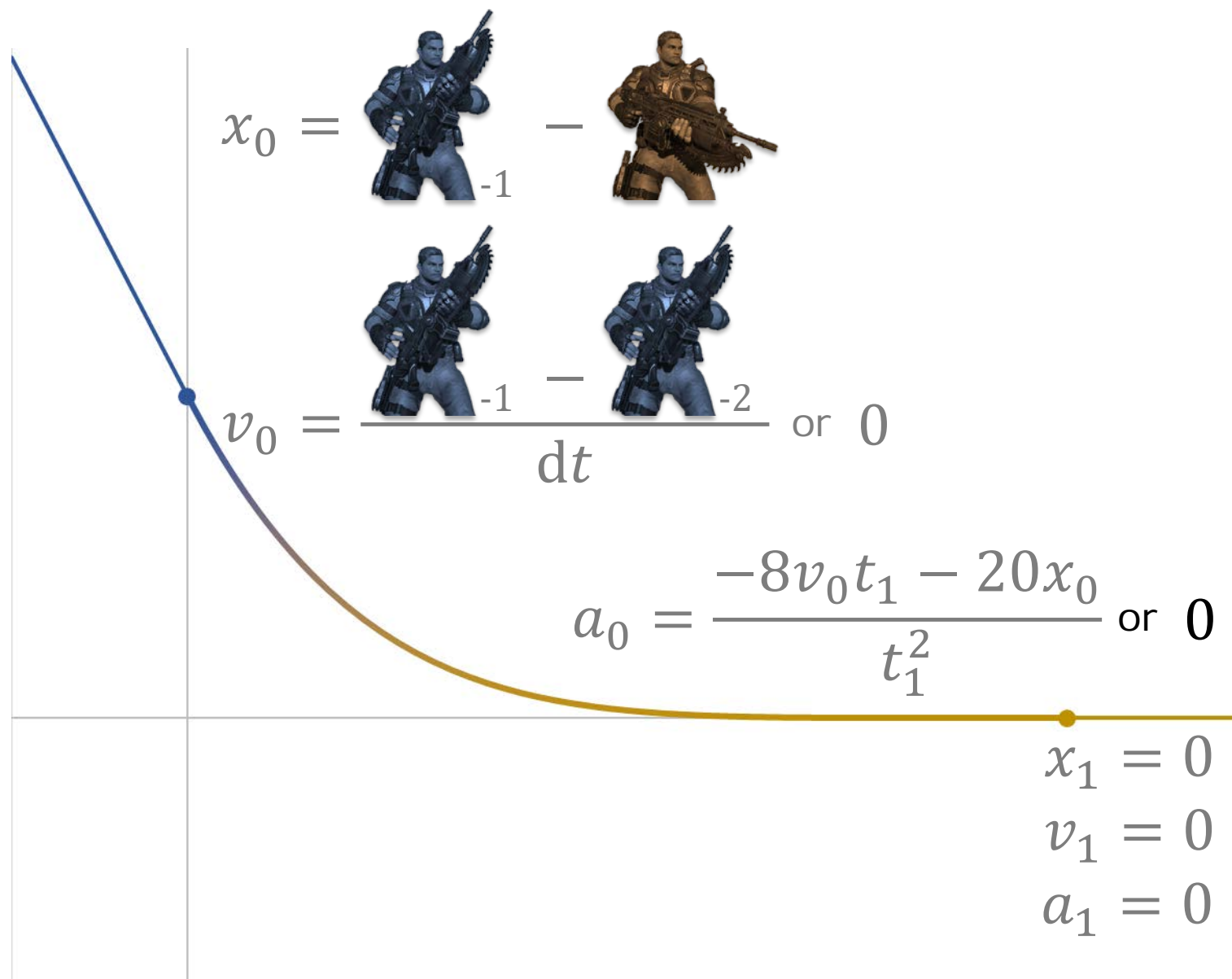
# INERTIALIZATION – ACCELERATION







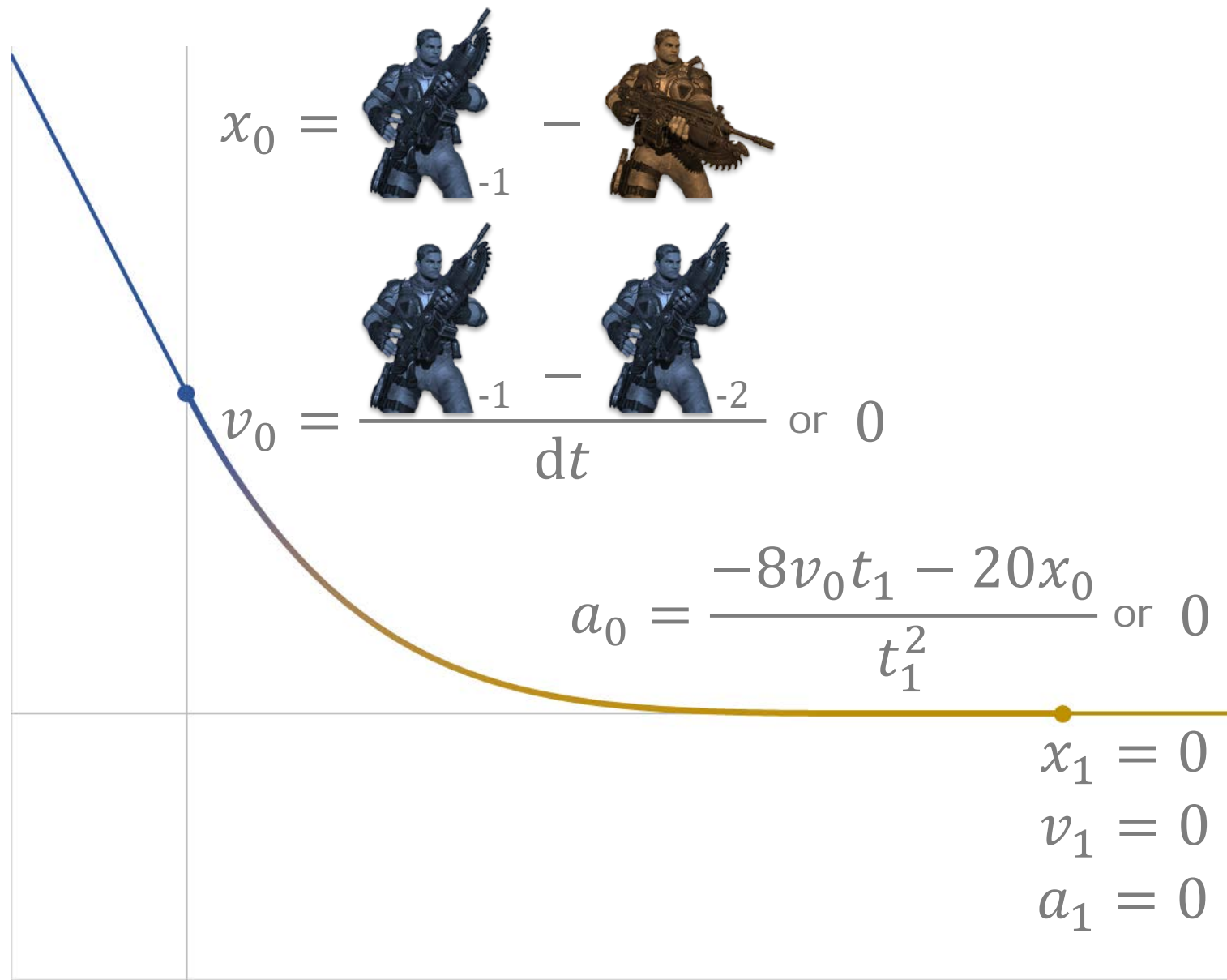
# INERTIALIZATION – ACCELERATION







# INERTIALIZATION – $x(t)$

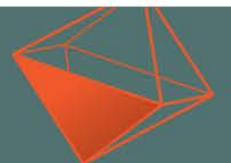


$$A = -\frac{a_0t_1^2 + 6v_0t_1 + 12x_0}{2t_1^5}$$

$$B = \frac{3a_0t_1^2 + 16v_0t_1 + 30x_0}{2t_1^4}$$

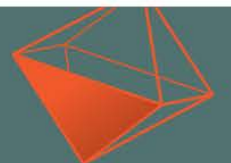
$$C = -\frac{3a_0t_1^2 + 12v_0t_1 + 20x_0}{2t_1^3}$$

$$x_t = At^5 + Bt^4 + Ct^3 + \frac{a_0}{2}t^2 + v_0t + x_0$$



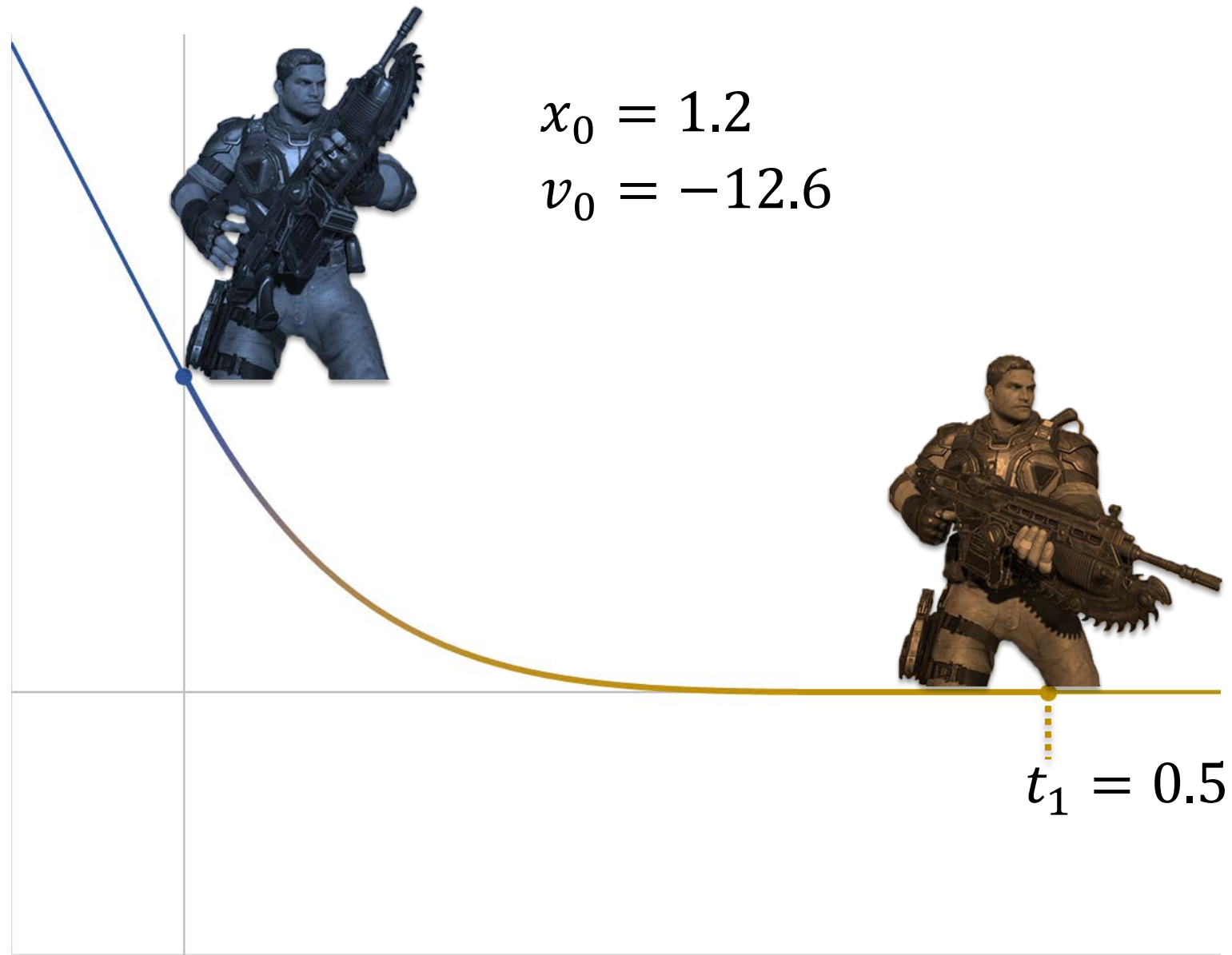


# OVERSHOOT REVISITED



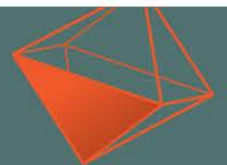
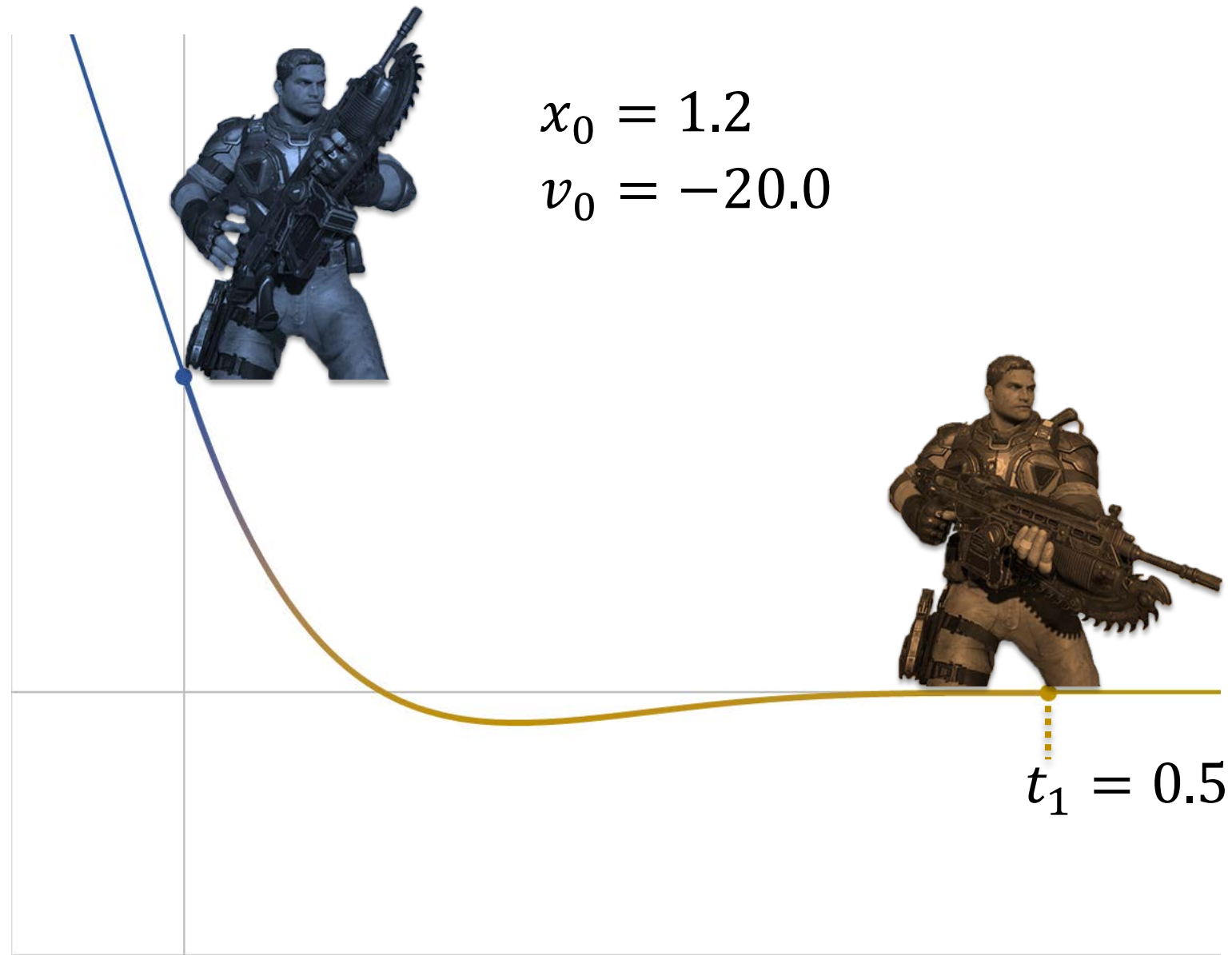


# OVERSHOOT REVISITED





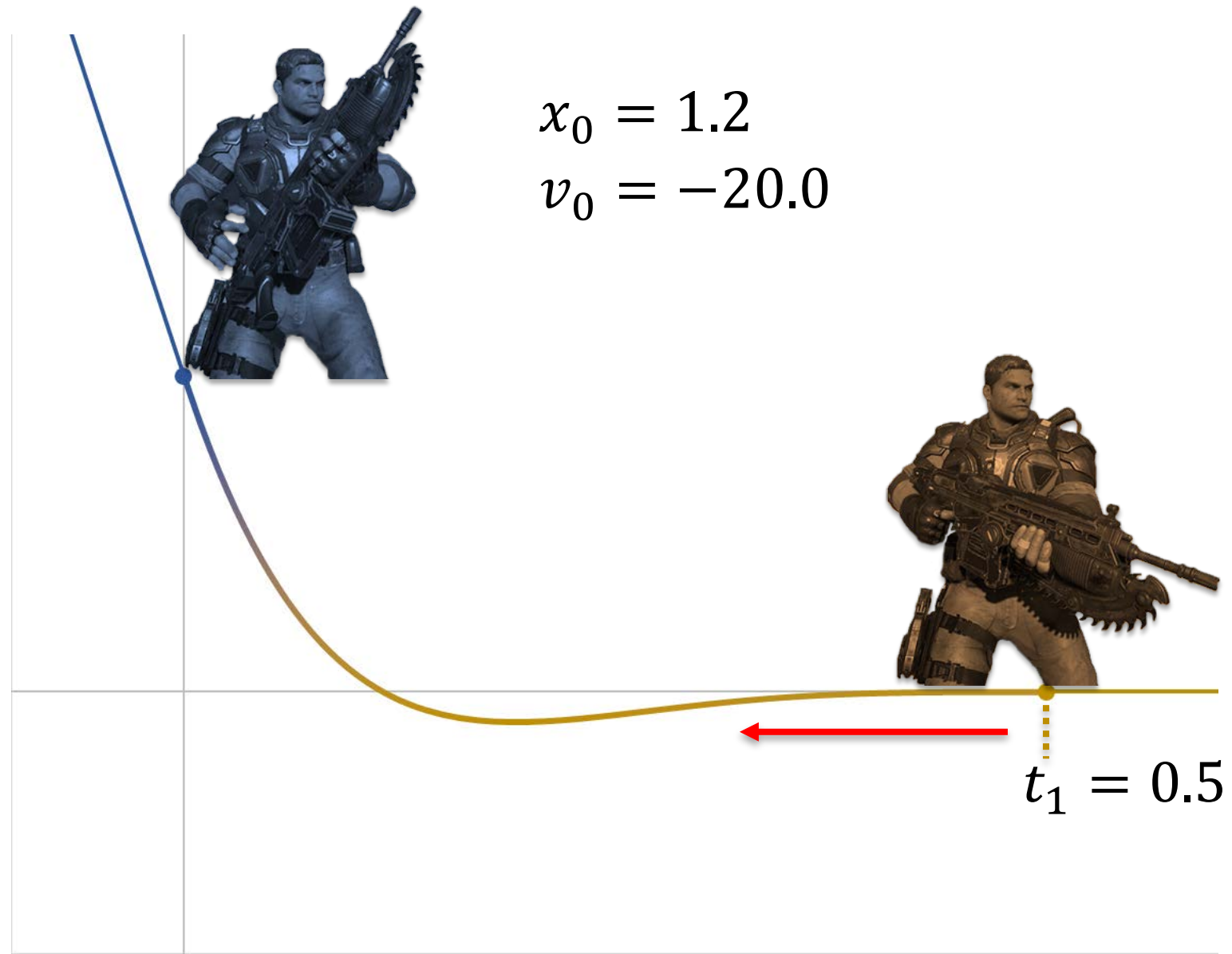
# OVERSHOOT REVISITED





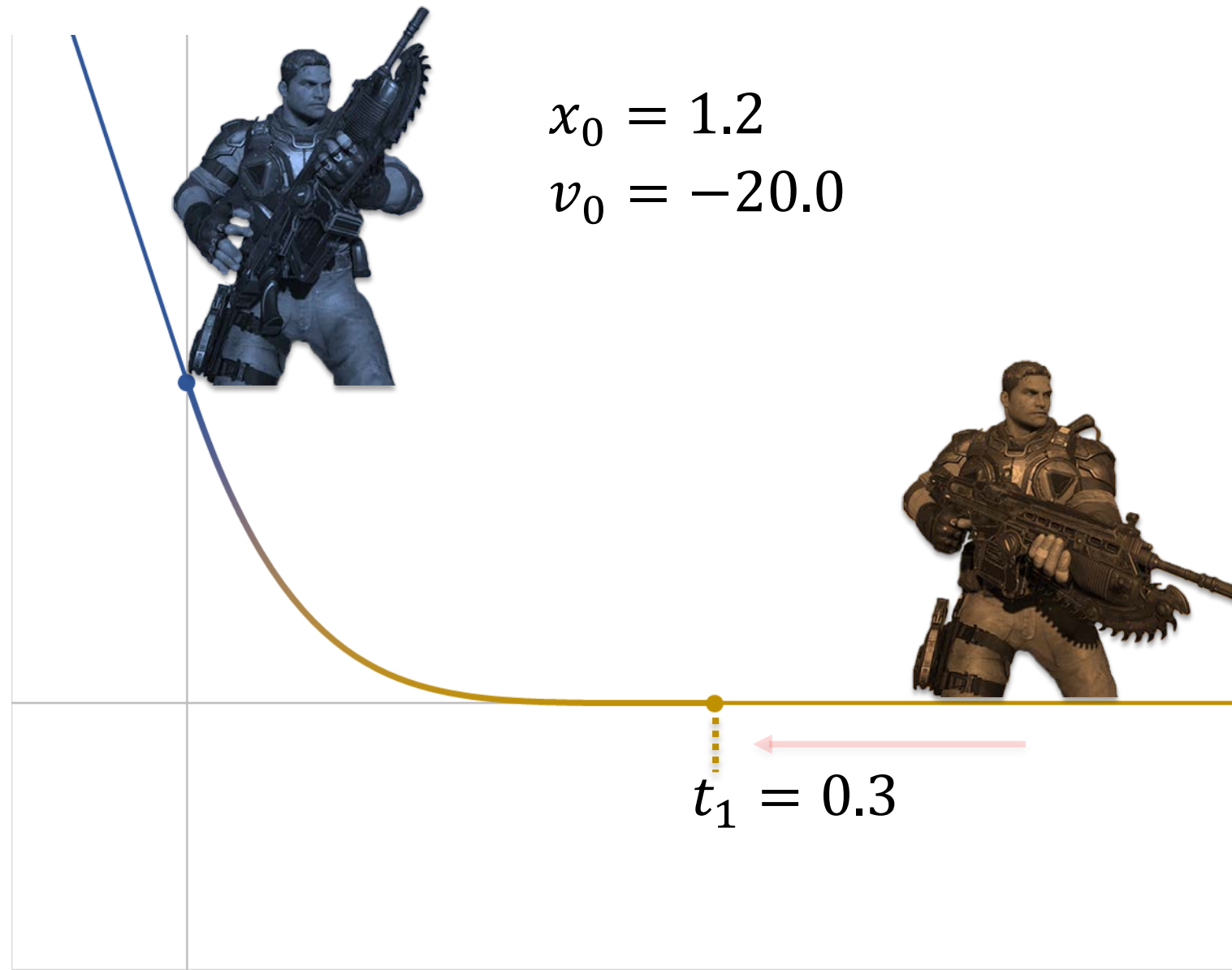


# IDEA #4: CLAMP TRANSITION TIME



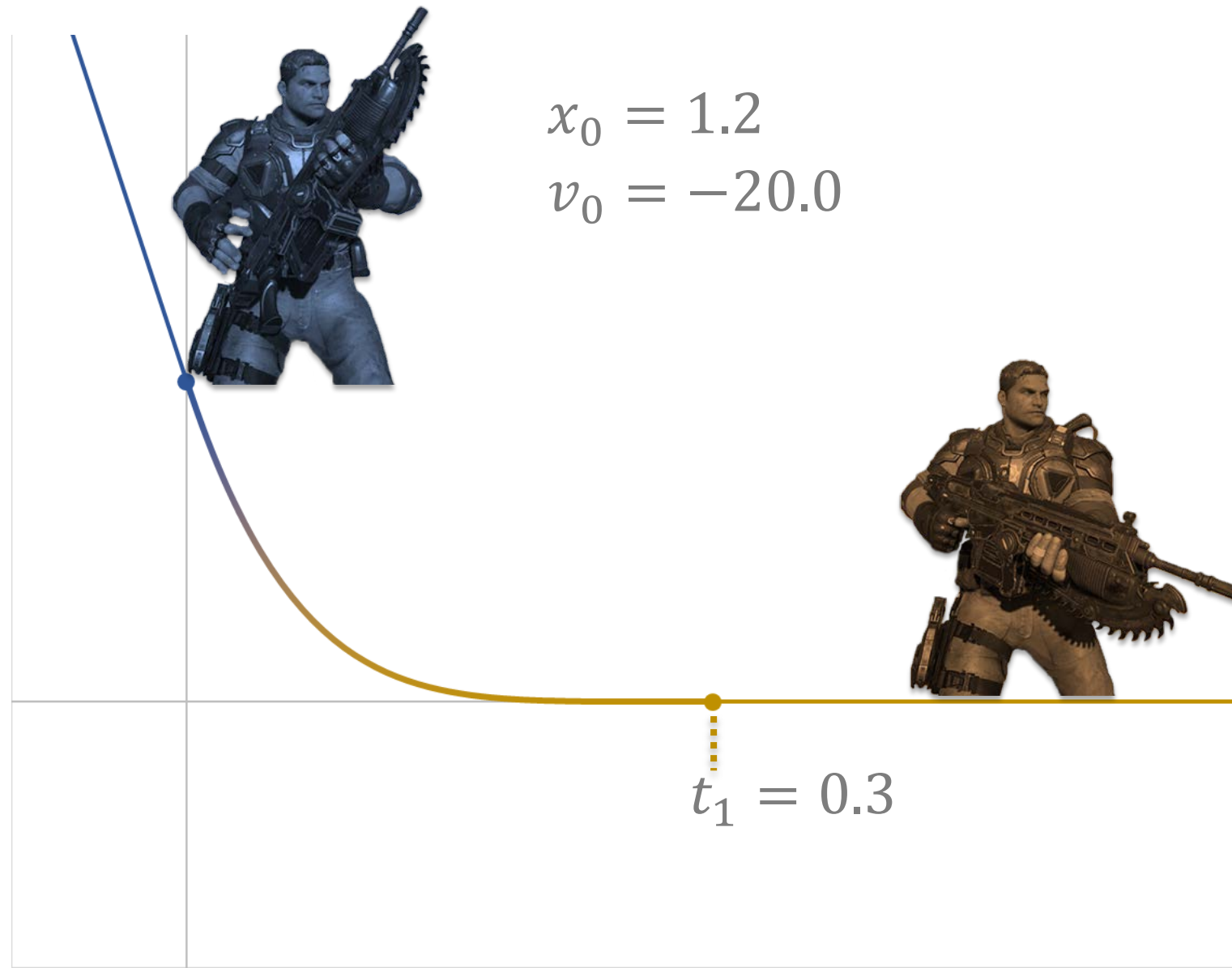


# IDEA #4: CLAMP TRANSITION TIME





# IDEA #4: CLAMP TRANSITION TIME

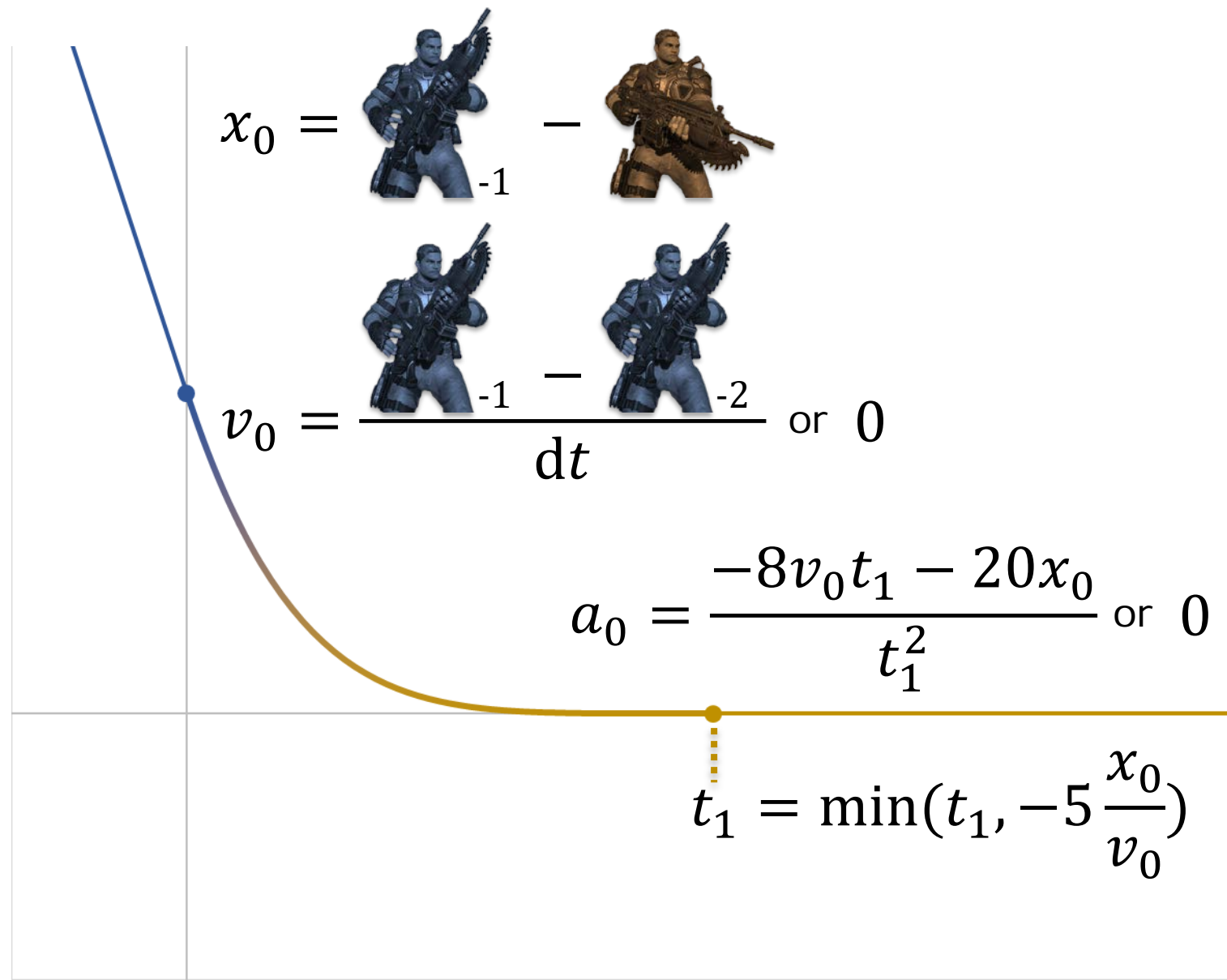


$$t_1 = \min(t_1, -5 \frac{x_0}{v_0})$$





# INERTIALIZATION ON ONE SLIDE



$$A = -\frac{a_0t_1^2 + 6v_0t_1 + 12x_0}{2t_1^5}$$

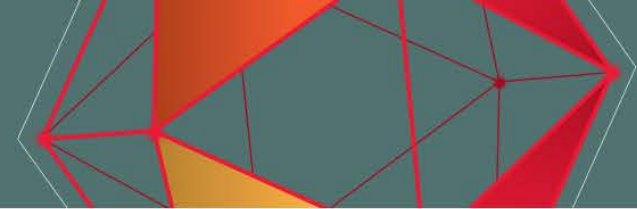
$$B = \frac{3a_0t_1^2 + 16v_0t_1 + 30x_0}{2t_1^4}$$

$$C = -\frac{3a_0t_1^2 + 12v_0t_1 + 20x_0}{2t_1^3}$$

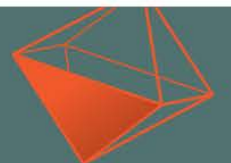
$$x_t = At^5 + Bt^4 + Ct^3 + \frac{a_0}{2}t^2 + v_0t + x_0$$







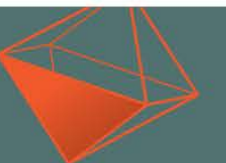
# VECTORS AND QUATERNIONS





# INERTIALIZING VECTORS

- Obvious choice:
  - Inertialize  $x, y, z$  independently
  - Visual artifacts if  $vx_0, vy_0, vz_0$  are too dissimilar (because of transition time clamping)
- Instead:
  - Decompose vector into direction and magnitude
  - Inertialize the magnitude





# INERTIALIZING VECTORS

$$\vec{x}_0 = \text{Soldier}_1 - \text{Soldier}_2$$

$$\vec{x}_{-1} = \text{Soldier}_2 - \text{Soldier}_3$$



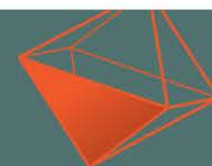


# INERTIALIZING VECTORS

$$\vec{x}_0 = \text{Soldier}_1 - \text{Soldier}_2$$

$$\vec{x}_{-1} = \text{Soldier}_1 - \text{Soldier}_2$$

$$x_0 = |\vec{x}_0|$$







# INERTIALIZING VECTORS

$$\vec{x}_0 = \text{Soldier}_1 - \text{Soldier}_2$$

$$x_0 = |\vec{x}_0|$$

$$\vec{x}_{-1} = \text{Soldier}_1 - \text{Soldier}_2$$

$$x_{-1} = \vec{x}_{-1} \cdot \frac{\vec{x}_0}{x_0}$$





# INERTIALIZING VECTORS

$$\vec{x}_0 = \text{Soldier}_0 - \text{Soldier}_{-1}$$

$$x_0 = |\vec{x}_0|$$

$$v_0 = \frac{x_0 - x_{-1}}{\Delta t}$$

$$\vec{x}_{-1} = \text{Soldier}_{-1} - \text{Soldier}_{-2}$$

$$x_{-1} = \vec{x}_{-1} \cdot \frac{\vec{x}_0}{x_0}$$





# INERTIALIZING VECTORS

$$\vec{x}_0 = \text{Soldier}_0 - \text{Soldier}_{-1}$$

$$x_0 = |\vec{x}_0|$$

$$v_0 = \frac{x_0 - x_{-1}}{\Delta t}$$

$$\vec{x}_t = x_t \frac{\vec{x}_0}{x_0} + \text{Soldier}_t$$

$$\vec{x}_{-1} = \text{Soldier}_{-1} - \text{Soldier}_{-2}$$

$$x_{-1} = \vec{x}_{-1} \cdot \frac{\vec{x}_0}{x_0}$$





# INERTIALIZING QUATERNIONS

- Similar construction to vectors:
  - Decompose quaternion into axis and angle
  - Inertialize the angle







# INERTIALIZING QUATERNIONS

$$q_0 = \text{Soldier}_1^{-1} * \text{Soldier}_2^{-1}$$

$$q_{-1} = \text{Soldier}_1^{-2} * \text{Soldier}_2^{-1}$$



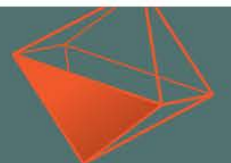


# INERTIALIZING QUATERNIONS

$$q_0 = \text{Soldier}_1^{-1} * \text{Soldier}_2^{-1}$$

$$q_{-1} = \text{Soldier}_1^{-2} * \text{Soldier}_2^{-1}$$

$$\vec{x}_0 = \text{Axis}(q_0) \quad x_0 = \text{Angle}(q_0)$$





# INERTIALIZING QUATERNIONS

$$q_0 = \text{[Soldier 1]}^{-1} * \text{[Soldier 2]}^{-1}$$

$$\vec{x}_0 = \text{Axis}(q_0) \quad x_0 = \text{Angle}(q_0)$$

$$q_{-1} = \text{[Soldier 1]}^{-2} * \text{[Soldier 2]}^{-1}$$

$$x_{-1} = 2 \tan^{-1} \frac{\overrightarrow{q_{xyz}} \cdot \vec{x}_0}{q_w}$$

Twist of  $q_{-1}$  around  $\vec{x}_0$

K. Shoemake. 1994.  
Fiber Bundle Twist Reduction  
Graphics Gems IV, 230 – 236





# INERTIALIZING QUATERNIONS

$$q_0 = \text{[Soldier 1]}^{-1} * \text{[Soldier 2]}^{-1}$$

$$\vec{x}_0 = \text{Axis}(q_0) \quad x_0 = \text{Angle}(q_0)$$

$$v_0 = \frac{x_0 - x_{-1}}{\Delta t}$$

$$q_{-1} = \text{[Soldier 1]}^{-2} * \text{[Soldier 2]}^{-1}$$

$$x_{-1} = 2 \tan^{-1} \frac{\overrightarrow{q_{xyz}} \cdot \vec{x}_0}{q_w}$$

Twist of  $q_{-1}$  around  $\vec{x}_0$

K. Shoemake. 1994.  
Fiber Bundle Twist Reduction  
Graphics Gems IV, 230 – 236







# INERTIALIZING QUATERNIONS

$$q_0 = \text{[Soldier]}^{-1} * \text{[Soldier]}^{-1}$$

$$\vec{x}_0 = \text{Axis}(q_0) \quad x_0 = \text{Angle}(q_0)$$

$$v_0 = \frac{x_0 - x_{-1}}{\Delta t}$$

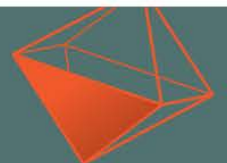
$$q_t = \left\{ \begin{array}{l} \text{Axis: } \vec{x}_0 \\ \text{Angle: } x_t \end{array} \right\} * \text{[Soldier]}_t$$

$$q_{-1} = \text{[Soldier]}^{-2} * \text{[Soldier]}^{-1}$$

$$x_{-1} = 2 \tan^{-1} \frac{\overrightarrow{q_{xyz}} \cdot \vec{x}_0}{q_w}$$

Twist of  $q_{-1}$  around  $\vec{x}_0$

K. Shoemake. 1994.  
Fiber Bundle Twist Reduction  
Graphics Gems IV, 230 – 236





# BLENDING VS INERTIALIZATION

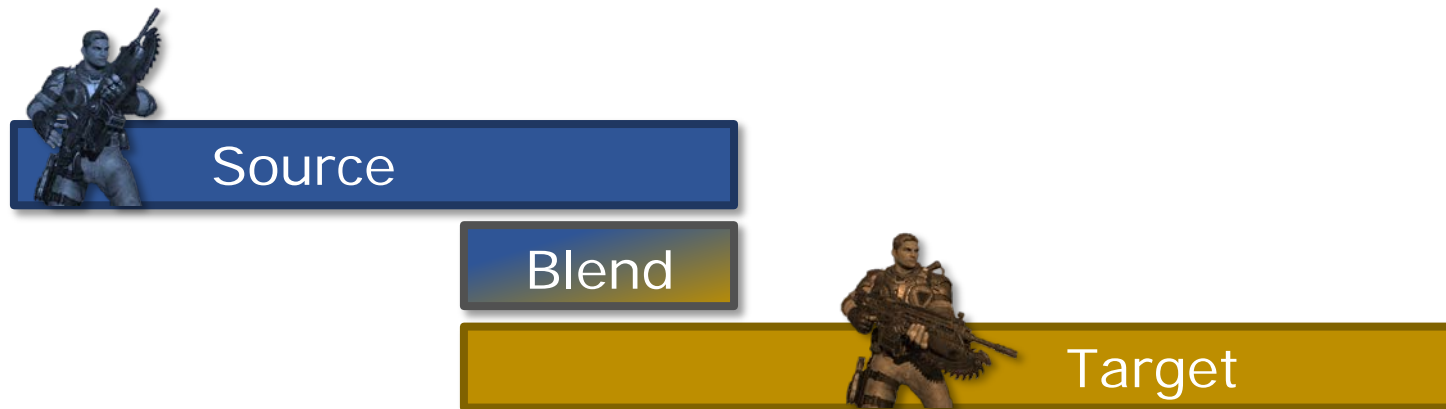




# BLENDING VS INERTIALIZATION

## Blending

- Evaluate both Source & Target during transition
- Variable anim frame cost



## Inertialization

- Only evaluate Target during transition
- Fixed anim frame cost

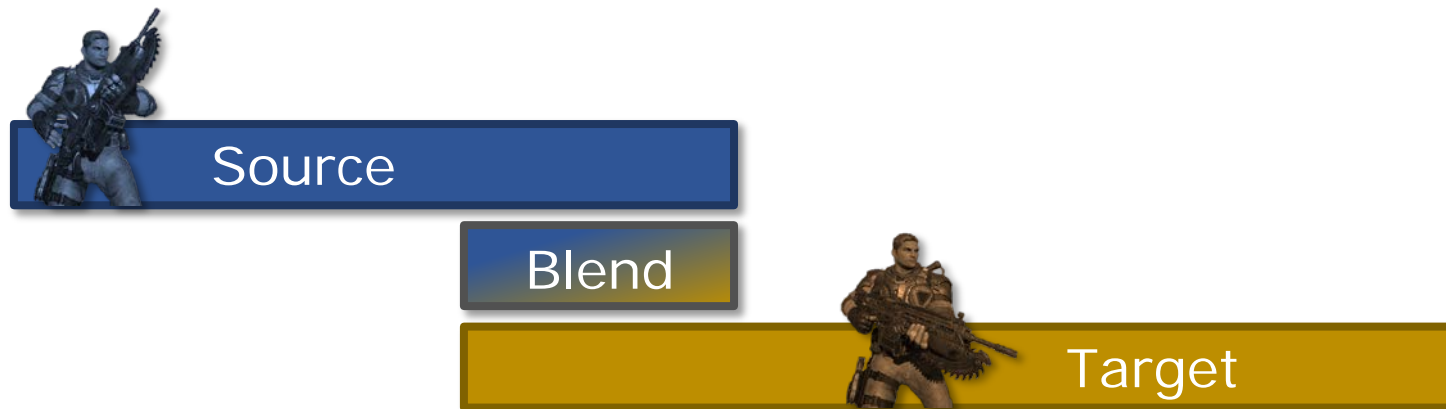




# BLENDING VS INERTIALIZATION

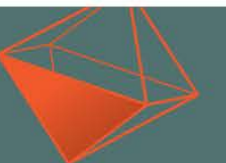
## Blending

- Manage multiple sets of state during transitions
- Adds complexity



## Inertialization

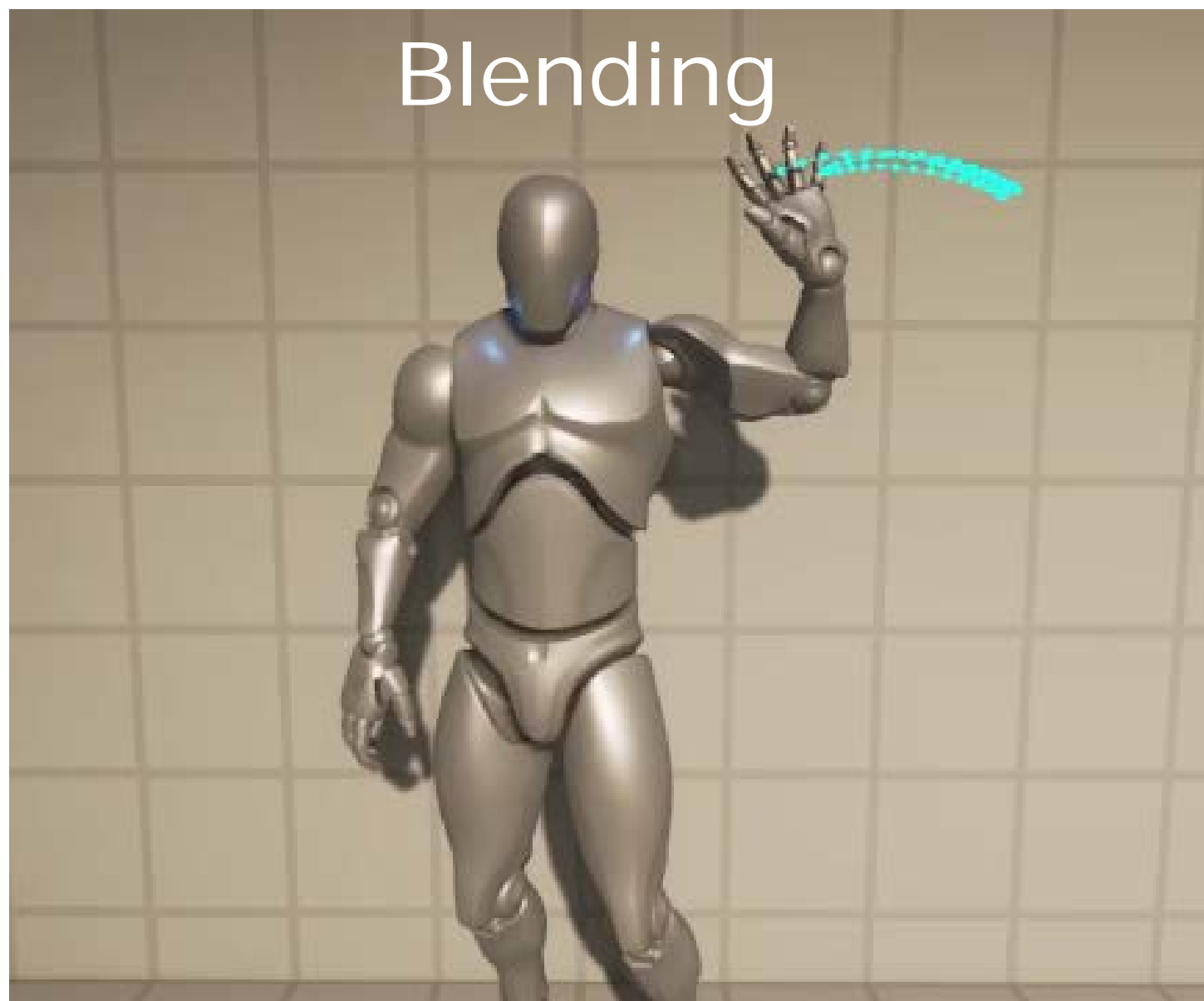
- Only maintain one set of state during transitions
- Fire and forget





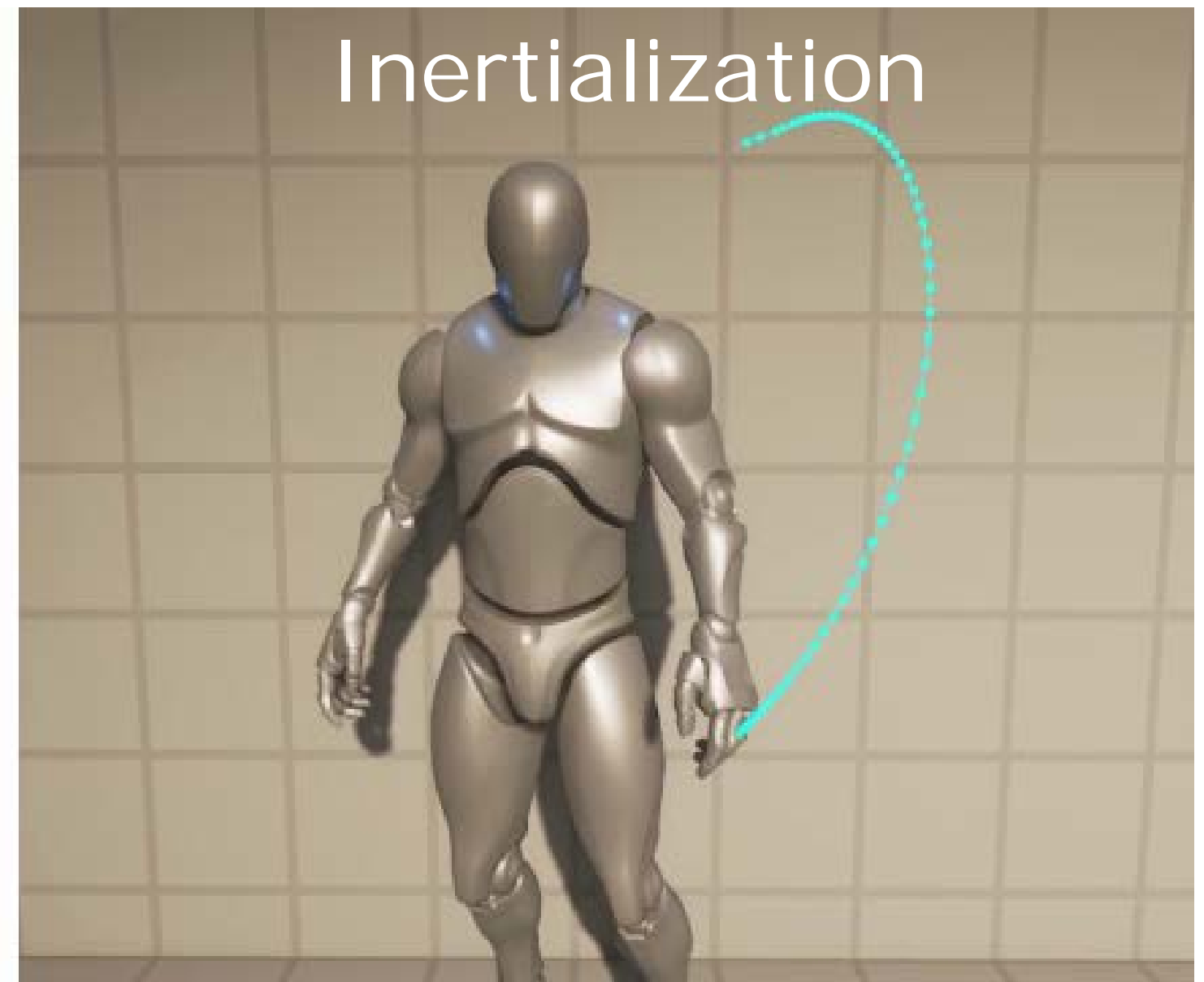
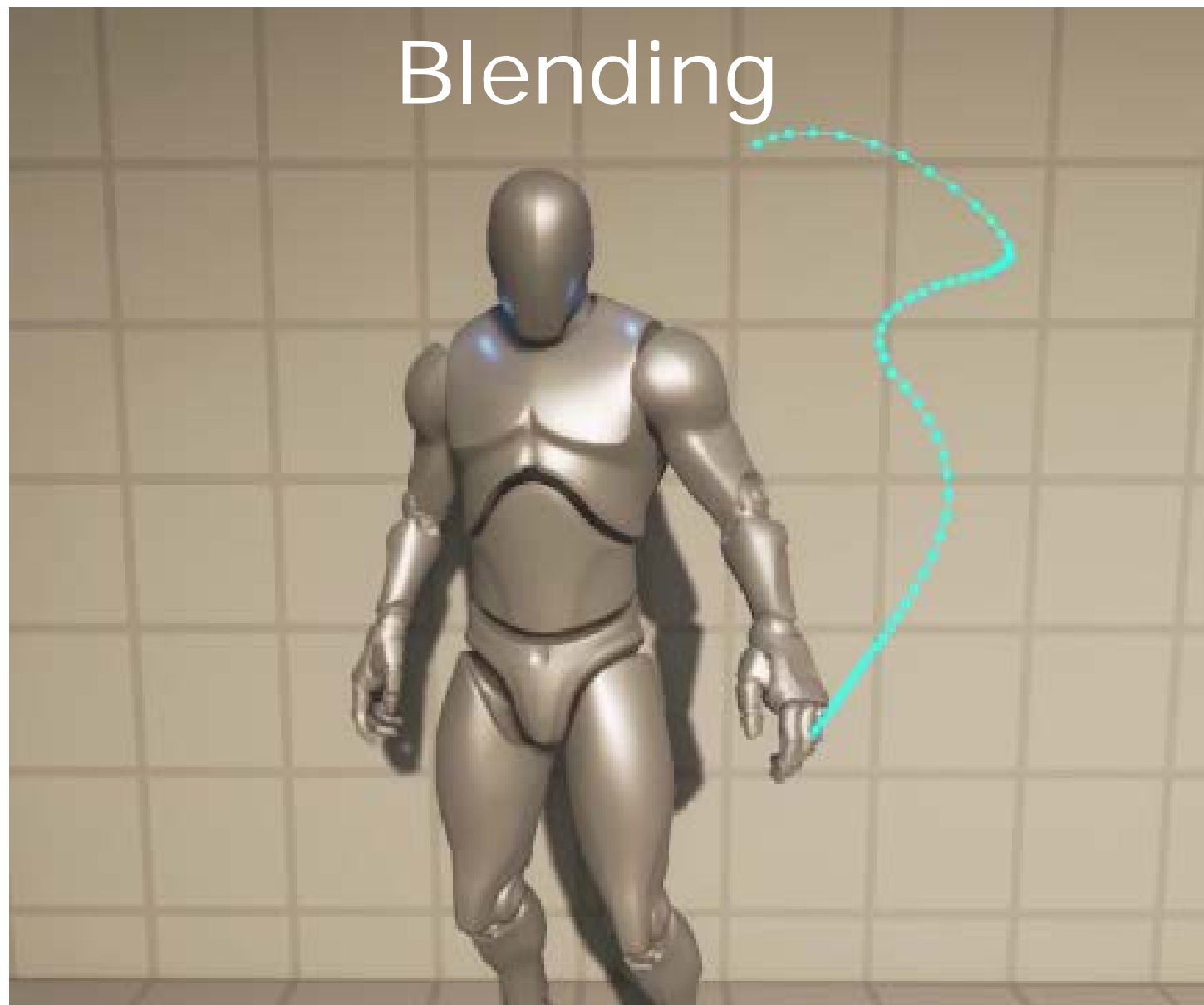


# BLENDING VS INERTIALIZATION



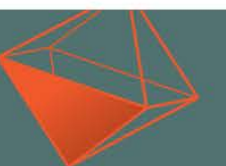


# BLENDING VS INERTIALIZATION





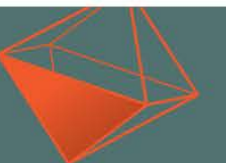
# INERTIALIZATION IN A GAME ENGINE





# INERTIALIZATION IN A GAME ENGINE

- Inertialization Node / Filter
- Animation System Hooks
- Code Hooks

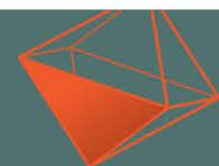
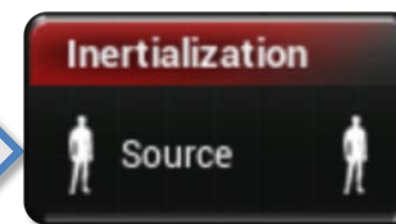
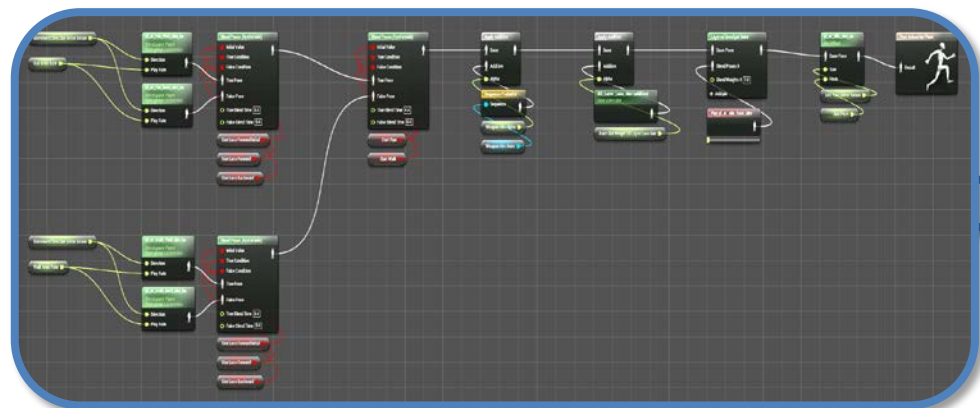






# INERTIALIZATION NODE

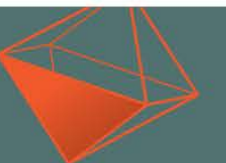
- Evaluated after the main animation graph
- Input is discontinuous pose stream
- Output is inertialized pose stream





# INERTIALIZATION NODE

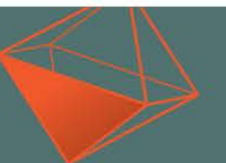
- When a new inertialization is requested:
  - Compute and store  $x_0$ ,  $v_0$  for all joints
  - Store  $t_1$  and set  $t = 0$
- Every frame:
  - Update  $t$  with delta time
  - Evaluate and apply  $x(t)$  for all joints
  - Store the OUTPUT pose in the pose history buffer





# ANIMATION SYSTEM HOOKS

- Add “inertialization” as a new blend curve type
- When a blend is requested with “inertialization” type:
  - Inertialize with the supplied blend time
  - Zero the blend time to bypass regular blending





# CODE HOOKS

- Expose “Request Inertialization” to code
- Eliminate other types of discontinuities
- And other tricks...



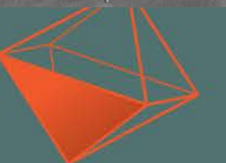




# TIPS AND TRICKS



Image Source: Evan Amos via Wikimedia Commons





# SMOOTHING OTHER DISCONTINUITIES

- Gears of War 3:
  - Snap character rotation when switching to sprint
- Gears of War 4:
  - Snap character rotation when switching to sprint
  - Inertialize away the discontinuity







# LOCOMOTION FILTERING

- Gears controls are very responsive (twitchy)
- Filter inputs to locomotion blend spaces
- If filtered values are too far from actual values...
  - Snap to actual values
  - Inertialize
- Fluid pose even with twitchy inputs





# FIRE & FORGET – MOTION WARPING

- Don't need to maintain warp point data across transitions
- Only 1 active warp at a time
- Simplifies bookkeeping
- Simplifies replication



S. Dickinson. Motion Warping in 'Gears of War 4': Doing More with Less. GDC 2017







# THANK YOU

## DAVID BOLLO

dbollo@microsoft.com

